

5. In electrolytic capacitors positive terminal is [1]
 a) one on which aluminium oxide film is not formed b) one on which aluminium oxide film is formed
 c) none of the these d) either of the two terminals
6. A wire of length L carrying current i is placed perpendicular to the magnetic induction B . The total force on the wire is [1]
 a) LB/i b) iL/B
 c) iLB d) iB/L
7. Inductance plays the role of [1]
 a) inertia b) friction
 c) force d) source of emf
8. The value of 1 Bohr magneton is: [Given $h = 6.62 \times 10^{-34}$ Js, $e = 1.6 \times 10^{-19}$ C and $m_e = 9.1 \times 10^{-31}$ kg] [1]
 a) 7.27×10^{-24} Am² b) 9.27×10^{-24} Am²
 c) 10.57×10^{-24} Am² d) 8.57×10^{-24} Am²
9. What happens to fringe width in the Young's double slit experiment, if it is performed in glycerine instead of air? [1]
 a) The fringes shrink b) The fringes disappear
 c) The fringes remain unchanged d) The fringes get enlarged
10. The attractive force between 2 charges is related to the distance between them as [1]
 a) r b) $\frac{1}{r^2}$
 c) $r^{\frac{1}{2}}$ d) $\frac{1}{r}$
11. Consider the junction diode as ideal. The value of current flowing through AB is [1]
-
- a) 10^{-2} A b) 0 A
 c) 10^{-1} A d) 10^{-3} A
12. Magnifying power of a microscope depends on [1]
 a) focal length of eyepiece and objective. b) colour of light.
 c) focal length of objective and color of light. d) focal length of eyepiece and color of light.
13. **Assertion (A):** The photoelectrons produced by a monochromatic light beam incident on a metal surface have a spread in their kinetic energies. [1]
Reason (R): The energy of electrons emitted from inside the metal surface, is lost in collision with the other atoms in the metal.
- a) Both A and R are true and R is the correct explanation of A. b) Both A and R are true but R is not the correct explanation of A.
 c) A is true but R is false. d) A is false but R is true.
14. **Assertion (A):** Positive charge always moves from a higher potential point to a lower potential point. [1]

Reason (R): Electric potential is a vector quantity.

- a) Both A and R are true and R is the correct explanation of A. b) Both A and R are true but R is not the correct explanation of A.
c) A is true but R is false. d) A is false but R is true.

15. **Assertion (A):** Interference pattern is made by using yellow light instead of red light, the fringes becomes narrower. [1]

Reason (R): In Young's double slit experiment, fringe width is given by $\beta = \frac{\lambda D}{d}$.

- a) Both A and R are true and R is the correct explanation of A. b) Both A and R are true but R is not the correct explanation of A.
c) A is true but R is false. d) A is false but R is true.

16. **Assertion (A):** An alternating current of frequency 50 Hz becomes zero, 100 times in one second. [1]

Reason (R): Alternating current changes direction and becomes zero twice in a cycle.

- a) Both A and R are true and R is the correct explanation of A. b) Both A and R are true but R is not the correct explanation of A.
c) A is true but R is false. d) A is false but R is true.

Section B

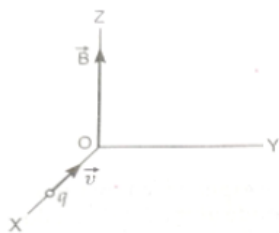
17. Gamma rays and radio waves travel with the same velocity in free space. Distinguish between them in terms of their origin and the main application. [2]

18. A straight solenoid of length 50 cm has 1000 turns and a mean cross-sectional area of $2 \times 10^{-4} \text{ m}^2$. It is placed with its axis at 30° , with a uniform magnetic field of 0.32 T. Find the torque acting on the solenoid when a current of 2A is passed through it. [2]

19. Draw the energy band diagram of (i) n-type, and (ii) p-type semiconductors at temperature $T > 0 \text{ K}$. [2]
In the case of n-type Si-semiconductor, the donor energy level is slightly below the bottom of conduction band whereas in p-type semiconductor, the acceptor energy level is slightly above the top of valence band. Explain, giving examples, what role do these energy levels play in conduction and valence bands.

20. In the first excited state of the hydrogen atom, its radius is found to be $21.2 \times 10^{-11} \text{ m}$. Calculate its Bohr radius in the ground state. Also, calculate the total energy of the atom in the second excited state. [2]

21. As shown in figure, a charge q moving along the X-axis with a velocity \vec{v} is subjected to a uniform magnetic field \vec{B} acting along the Z-axis as it crosses the origin O. [2]



- i. Trace its trajectory.
ii. Does the charge gain kinetic energy, as it enters the magnetic field? Justify your answer.

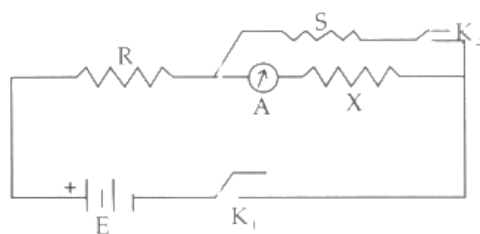
OR

Depict the field-line pattern due to a current-carrying solenoid of finite length.

- i. In what way do these lines differ from those due to an electric dipole?
ii. Why can't two magnetic field lines intersect each other?

Section C

22. The reading of the (ideal) ammeter, in the circuit shown here, is equal too. [3]



- i. I when key K_1 is closed but key K_2 is open.
- ii. $\frac{I}{2}$ when both keys K_1 and K_2 are closed.

Find the expression of the resistance of X in terms of the resistances of R and S.

23. Draw the circuit diagram showing how a p-n junction diode is [3]

- i. forward biased
- ii. reverse biased

How is the width of depletion layer affected in the two cases?

24. Red light, however bright it is, cannot produce the emission of electrons from a clean zinc surface. But even weak ultraviolet radiation can do so. Why? [3]

Electrons are emitted from the cathode of negligible work function, when photons of wavelength λ are incident on it. Derive the expression for the de Broglie wavelength of the electrons emitted in terms of the wavelength of the incident light.

25. i. Draw a plot showing the variation of potential energy of a pair of nucleons as a function of their separation. [3]

Mark the regions where the nuclear force is

- a. attractive and
- b. repulsive.

ii. In the nuclear reaction ${}_0n^1 + {}_{92}^{235}\text{U} \rightarrow {}_a^X\text{Xe} + {}_b^{94}\text{Sr} + 2{}_0n^1$ determine the values of a and b.

26. Hydrogen atom in its ground state is excited by means of monochromatic radiation of wavelength 975\AA . [3]

- i. How many different lines are possible in the resulting spectrum?
- ii. Calculate the longest wavelength amongst them. You may assume the ionization energy for hydrogen atom as 13.6 eV.

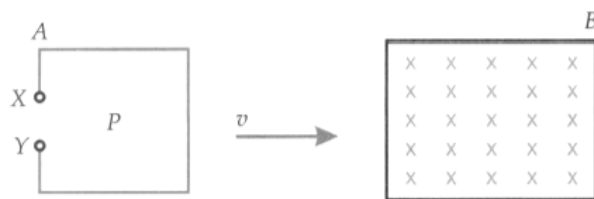
27. How is the spacing between fringes in a double slit experiment affected if: [3]

- a. the slits separation is increased,
- b. the colour of light used is changed from red to blue,
- c. the whole apparatus is submerged in a oil of refractive index 1.2?

Justify your answer in each case.

28. A rectangular coil P is moved from a point A to another point B with uniform velocity 'v' through a region of a [3]

uniform magnetic field acting normally inwards as shown in the figure. Show graphically (i) the variation of magnetic flux associated with the coil with time, (ii) the variation of induced emf across points X and Y of the coil with time.

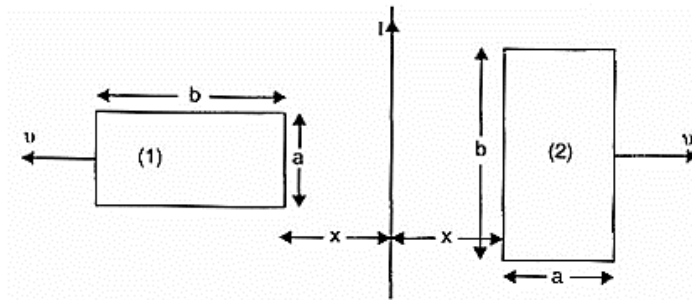


Explain the nature of variation in magnetic flux as represented by the graph in the first case.

OR

The figure shows two identical rectangular loops (1) and (2) placed on a table along with a straight long current carrying conductor between them.

- What will be the directions of the induced current in the loops when they are pulled away from the conductor with same velocity v ?
- Will the emf induced in the two loops be equal?

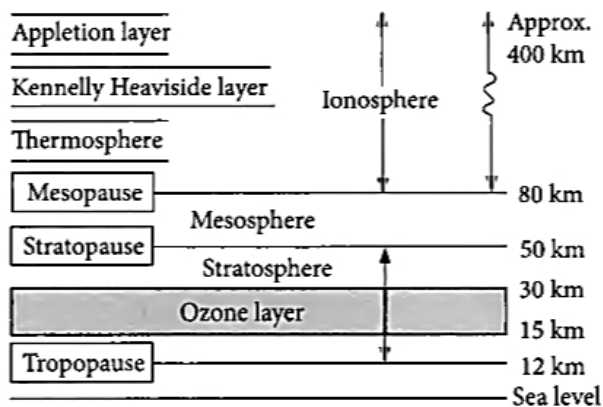


Section D

29. Read the text carefully and answer the questions:

[4]

Radio waves are produced by the accelerated motion of charges in conducting wires. Microwaves are produced by special vacuum tubes. Infrared waves are produced by hot bodies and molecules also known as heat waves. UV rays are produced by special lamps and very hot bodies like Sun.



- Solar radiation is
 - transverse electromagnetic wave
 - longitudinal electromagnetic waves
 - both longitudinal and transverse electromagnetic waves
 - none of these.
 - Option (i)
 - Option (iv)
 - Option (iii)
 - Option (ii)
- What is the cause of greenhouse effect?
 - Ultraviolet rays
 - X-rays
 - Infrared rays
 - Radiowaves

- (c) Biological importance of ozone layer is
- a) it stops ultraviolet rays
 - b) none of these.
 - c) it reflects radiowaves
 - d) It layer reduces greenhouse effect

OR

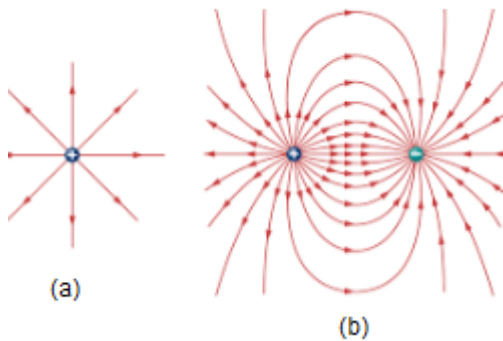
Ozone is found in

- a) troposphere
 - b) mesosphere
 - c) ionosphere
 - d) stratosphere
- (d) Earth's atmosphere is richest in
- a) ultraviolet
 - b) infrared
 - c) X-rays
 - d) microwaves

30. **Read the text carefully and answer the questions:**

[4]

Electric field lines as a path, straight or curved in an electric field such that tangent to it at any point gives the direction of electric field intensity at the point. Electric field lines are continuous curves they start from a positive charged body and end at the negatively charged body. (Refer image)



- (a) Electric field due to a single charge is:
- a) cylindrically symmetric
 - b) symmetric
 - c) asymmetric
 - d) spherically symmetric
- (b) The SI unit of electric field intensity is:
- a) N/C
 - b) N
 - c) C/m²
 - d) N/m²
- (c) Pick the wrong statement.
- a) Electric field lines are continuous curves.
 - b) Electric field lines can intersect each other.
 - c) Electric field lines are always normal to the surface of a conductor.
 - d) The electrostatic field does not form a closed loop.
- (d) A metallic sphere is placed in a uniform electric field as shown in the figure. Which path is followed by electric field lines?

impedance of the circuit. Plot a graph to show the variation of current with frequency of the source, explaining the nature of its variation.

OR

- a. Derive an expression for the impedance of a series L-C-R circuit connected to an AC supply of variable frequency.
- b. Explain briefly how the phenomenon of resonance in the circuit can be used in the tuning mechanism of a radio or a TV set?

Solution

Section A

1. (a) $n_i e (\mu_e + \mu_h) E$

Explanation: $I = I_e + I_h = en_e Av_e + en_h Av_h$

$$= eA (n_e \mu_e + n_h \mu_h) E$$

$$j = \frac{I}{A} = en_i (\mu_e + \mu_h) E$$

2.

(d) remains the same

Explanation: Neutral temperature is independent of temperature of cold junction.

3.

(b) 3.00

Explanation: Here, $\lambda = 5,000 \text{ \AA} = 5 \times 10^{-7} \text{ m}$ and $\nu = 2 \times 10^{14} \text{ Hz}$

Therefore, speed of light in the material,

$$v = \nu \lambda = 2 \times 10^{14} \times 5 \times 10^{-7} = 10^8 \text{ ms}^{-1}$$

Hence, the refractive index of the material,

$$\mu = \frac{c}{v} = \frac{3 \times 10^8}{10^8} = 3$$

4.

(d) 4.48 T

Explanation: $B = \frac{\mu_0 \mu_r Ni}{2\pi r} = \frac{4\pi \times 10^{-7} \times 800 \times 3500 \times 1.2}{2\pi \times 15 \times 10^{-2}} = 4.48 \text{ T}$

5.

(b) one on which aluminium oxide film is formed

Explanation: Aluminium electrolytic capacitors have the Aluminium foil anode (positive terminal) which is etched and covered with a layer of Aluminium Oxide which acts as a dielectric. The whole assembly is covered using a paper separator soaked in electrolyte such as, Borax or Glycol and covered by Aluminium foil which acts as cathode (negative electrode)

6.

(c) iLB

Explanation: Magnitude of the Force experienced by a current carrying conductor placed in a magnetic field is $iLB \sin \theta$.

If the angle between the directions of the current and the magnetic field is 90° , $F = iLB$

7.

(a) inertia

Explanation: inertia

8.

(b) $9.27 \times 10^{-24} \text{ Am}^2$

Explanation: 1 Bohr magneton

$$= \frac{eh}{4\pi m_e}$$

$$= \frac{1.6 \times 10^{-19} \times 6.62 \times 10^{-34}}{4\pi \times 9.1 \times 10^{-31}}$$

$$= 9.27 \times 10^{-24} \text{ Am}^2$$

9.

(a) The fringes shrink

Explanation: The fringes shrink

10.

(b) $\frac{1}{r^2}$

Explanation: According to Coulomb's law the force between two charges is inversely proportional to the square of distance between the two charges. So $F \propto \frac{1}{r^2}$.

11. (a) 10^{-2} A

Explanation: An ideal diode does not offer any resistance during forward biasing.

$$\therefore I = \frac{V_A - V_B}{R}$$

$$= \frac{4 - (-6)}{1000} \text{ A} = 10^{-2} \text{ A}$$

12. (a) focal length of eyepiece and objective.

Explanation: Magnification $\frac{m \propto 1}{f_o f_e}$

So, magnifying power of a microscope depends on focal length of eyepiece and objective only.

13. (a) Both A and R are true and R is the correct explanation of A.

Explanation: Photoelectrons produced by monochromatic light have different velocities and hence different energies. Actually all the electrons do not occupy the same level of energy. So, electrons coming out from different levels have different velocities and hence different energies. So, the assertion is true. The electrons coming out from inside the metal surface, face collisions with the other atoms in the metal. So, energies become different. Hence the reason is true and it explains the assertion.

14.

(c) A is true but R is false.

Explanation: If two points P and Q in an electric field are separated by an infinitesimal distance Δx and have a potential difference ΔV

between them, $E = \frac{-\Delta V}{\Delta x}$. Here, negative sign implies that \vec{E} has got a direction opposite to the potential gradient, i. e., in the direction of \vec{E} , the potential decreases, i. e., positive charge always moves from a higher potential point to a lower potential point.

15. (a) Both A and R are true and R is the correct explanation of A.

Explanation: Both A and R are true and R is the correct explanation of A.

16.

(b) Both A and R are true but R is not the correct explanation of A.

Explanation: Both A and R are true but R is not the correct explanation of A

Section B

| 17. | Gamma rays | Radio waves |
|-------------|---|--|
| Origin | Nuclear decay | Lightning |
| | From hottest and most energetic objects in the universe, such as neutron stars, pulsars, supernova explosions, and regions around black holes | From broadcast radio towers, cell phones and radars. |
| Application | In radiotherapy, sterilisation and disinfection | In fixed and mobile radio communication, radar and other navigation systems, communication satellites, computer networks |

18. Torque of solenoid is given by

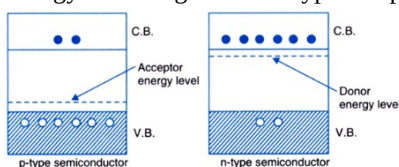
$$\tau = MB \sin \theta$$

$$= (NIA) B \sin \theta$$

$$= 1000 \times 2 \times 2 \times 10^{-4} \times 0.32 \times \frac{1}{2}$$

$$= 0.064 \text{ Nm}$$

19. Energy band diagrams of n-type and p-type semiconductors are shown below:



In the case of n-type semiconductors, The Donor energy level decreases the energy gap between the conduction band and the valence band, electrons from donor impurity atoms will move into the conduction band with a very small supply of energy. Hence, the conduction band will, therefore, have electrons as majority charge carriers. In the case of p-type semiconductor, a very small supply of energy can cause an electron from its valence band to jump to the acceptor energy level. Hence, the valence band will have a dominant density of holes which shows that holes are the majority charge carriers in p-type semiconductors.

20. $r_0 = 21.2 \times 10^{-11} \text{ m}$

First excited state means, $n = 2$

$$r_0 = n^2 r_1$$

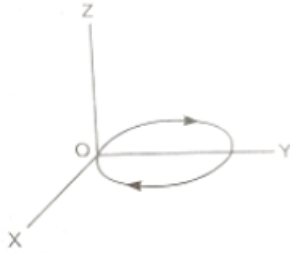
$$\text{or } r_1 = \frac{r_0}{n^2}$$

$$r_1 = \frac{21.2 \times 10^{-11}}{4} \text{ m}$$

$$= 5.3 \times 10^{-11} \text{ m}$$

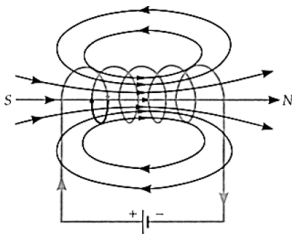
$$E = -\frac{13.6}{n^2} = -3.4 \text{ eV, hence total energy of atom is given by :- } -3.4 \text{ eV}$$

21. i. As the charged particle crosses the origin O with velocity \vec{v} (along negative X-axis), it comes under the effect of magnetic field \vec{B} (acting along positive Z-axis). A force equal to $\vec{F} = q(\vec{v} \times \vec{B})$ acts on the charged particle positive Y-axis. As a result, the particle moves along a circular path in XY-plane as shown in figure.



- ii. The force on the charged particle due to magnetic field is always perpendicular to its path and therefore, work done by magnetic field on the moving charge is zero. Hence, the charged particle will not gain kinetic energy.

OR



- i. The magnetic lines of force of a solenoid form closed loops while the electric lines of force of an electric dipole start from the positive charge and end at the negative charge.
- ii. Such curves are called magnetic lines of force. No two such lines of force can intersect. If they do so, then there will be two tangents and hence two directions of the magnetic field at the point of intersection which is impossible.

Section C

22. i. Current I when K_2 is open

$$I = \frac{E}{R+X}$$

- ii. Current I' when K_2 is closed

$$I' = \frac{E}{R + \left(\frac{SX}{S+X}\right)} = \frac{E(S+X)}{R(S+X) + SX} \quad (\text{so, S and X are parallel})$$

Current flowing through X, ($I' = I/2$)

$$\frac{I}{2} = \frac{I'S}{S+X} = \frac{ES}{R(S+X) + SX} \quad (\text{by putting the value of I, we get})$$

$$\Rightarrow \frac{E}{2(R+X)} = \frac{ES}{R(S+X) + SX}$$

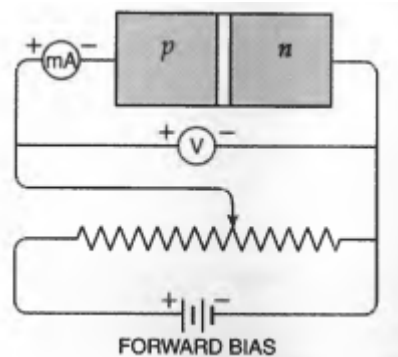
$$\Rightarrow 2(R+X)S = R(S+X) + SX$$

$$2RS + 2XS = RS + RX + SX$$

$$RS = RX - SX$$

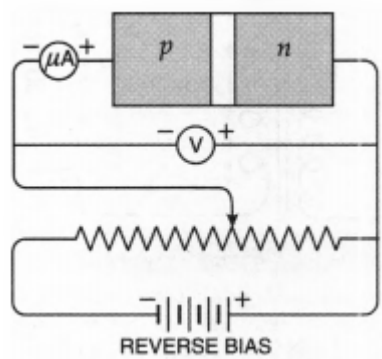
$$X = \frac{RS}{(R-S)}$$

23. i. The forward-bias connections of a p-n junction are as shown in Fig.



When the p-n junction is forward biased, the depletion layer becomes thin. It is because, the polarity of the external d.c. source opposes the fictitious battery developed across the junction. As a result, the potential drop across the junction decreases making the depletion layer thin. It leads to the low resistance of the junction diode during forward bias.

ii. The reverse-bias connections of a p-n junction are as shown in Fig.



When the p-n junction is reverse biased, the depletion layer becomes thick. It is because, the external d.c. source aids the fictitious battery. It results in the increase of potential drop across the junction and the depletion layer appears thick. Because of the increased thickness of the depletion layer, the p-n junction offers high resistance during reverse bias.

24. The frequency of ultraviolet radiations is more while that of red light is less than the threshold frequency for a zinc surface, so ultraviolet radiations can cause the emission of electrons and red light cannot.

From Einstein's photoelectric equation, K.E. of a photoelectron is

$$\frac{1}{2} m v^2 = h \nu - W_0 = h \nu - 0 = \frac{h c}{\lambda}$$

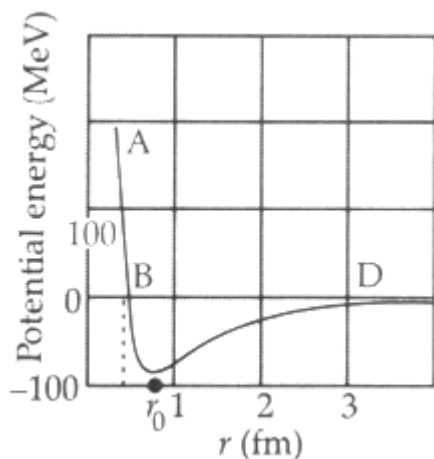
$$\text{or } v = \sqrt{\frac{2 h c}{m \lambda}}$$

de Broglie wavelength of electrons,

$$\lambda_e = \frac{h}{m v}$$

$$= \frac{h}{m} \sqrt{\frac{m \lambda}{2 h c}} = \sqrt{\frac{h \lambda}{2 m c}}$$

25. i.



For $r > r_0$, the force is attractive

For $r < r_0$, the force is repulsive

ii. We have, In nuclear reactions , mass no .is conserved Hence ,

$$1 + 235 = a + 94 + 2 \times 1$$

$$\therefore a = 236 - 96 = 140$$

In nuclear reactions , charge no. is conserved .so $0 + 92 = 54 + b + 2 \times 0$

$$\therefore b = 92 - 54 = 38$$

26. i. Energy of the ground state ($n = 1$) = - (ionization energy) = -13.6 eV

The wavelength of the incident radiation, $\lambda = 975 \text{ \AA}$

\therefore The energy of the incident photon = hc/λ

$$= \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{975 \times 10^{-10} \times 1.6 \times 10^{-19}} = 12.75 \text{ eV}$$

Let electron is excited to nth orbit,

$$\Rightarrow 12.75 = 13.6 \left(\frac{1}{1^2} - \frac{1}{n^2} \right)$$

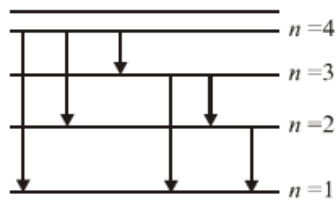
$$\Rightarrow n = 4$$

The quantum transitions to the less excited states gives six possible lines as follows:

$n = 4$: ($4 \rightarrow 3$), ($4 \rightarrow 2$), ($4 \rightarrow 1$)

$n = 3$: ($3 \rightarrow 2$), ($3 \rightarrow 1$)

$n = 2$: ($2 \rightarrow 1$)



ii. The longest wavelength emitted is for the transitions ($4 \rightarrow 3$) where energy difference is minimum.

$$E_{\min} = (E_4 - E_3) = 13.6 \left(\frac{1}{3^2} - \frac{1}{4^2} \right) = 0.661 \text{ eV}$$

$$\begin{aligned} \text{Thus } \lambda_{\max} &= \frac{hc}{E_{\min}} \\ &= \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{0.661 \times 1.6 \times 10^{-19}} \text{ m} \\ &\approx 18807 \text{ \AA} \end{aligned}$$

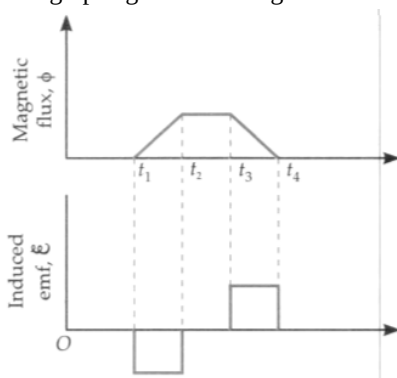
$$27. \beta = n \frac{\lambda D}{d}$$

a. As d increases, β decreases so spacing between fringes also decreases.

b. As λ decreases, β also decreases so spacing between fringes also decreases.

c. As whole apparatus is submerged in oil, λ decreases So β decreases and spacing between fringes will be narrow.

28. The graphs given in the figure show the variation of flux ϕ with time t and induced emf ε with time t , respectively.



Explanation of variation of magnetic time. Magnetic flux is proportional to the coil linked with flux. Initially, the coil lies magnetic field, flux through it is zero. As the field at time t_1 the flux begins to increase. with time. Between times t_2 and t_3 , in the magnetic field, so flux remains: After this the flux decreases linearly with reduces to zero at time t_4 , when the coil co the magnetic field.

OR

i. The direction of induced current will be such that it tends to maintain the original flux. So induced current flows anticlockwise in loop 1 and clockwise in loop 2.

ii. No, the emf's induced in the two loops will not be equal.

Since, the rate of change of flux is more in the second coil, emf induced in the second coil is more than that in the first coil.

Emf in the first coil, $E_1 = Bav$

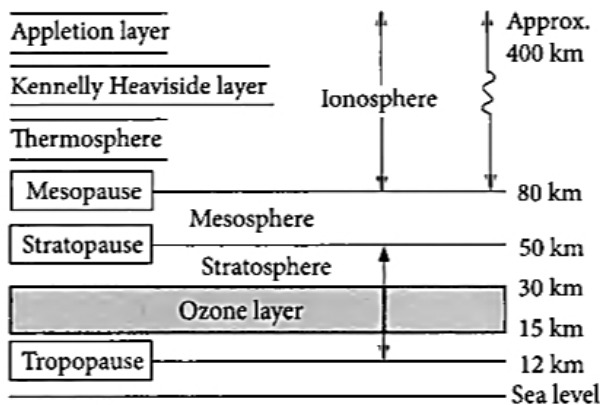
Emf in the school coil, $E_2 = Bbv$

Since, $b > a$ therefore, $E_2 > E_1$

Section D

29. Read the text carefully and answer the questions:

Radio waves are produced by the accelerated motion of charges in conducting wires. Microwaves are produced by special vacuum tubes. Infrared waves are produced by hot bodies and molecules also known as heat waves. UV rays are produced by special lamps and very hot bodies like Sun.



(i) (a) Option (i)

Explanation: transverse electromagnetic wave

(ii) (c) Infrared rays

Explanation: Greenhouse effect is due to infrared rays.

(iii) (a) it stops ultraviolet rays

Explanation: Ozone layer absorbs the harmful ultraviolet radiations coming from the sun.

OR

(d) stratosphere

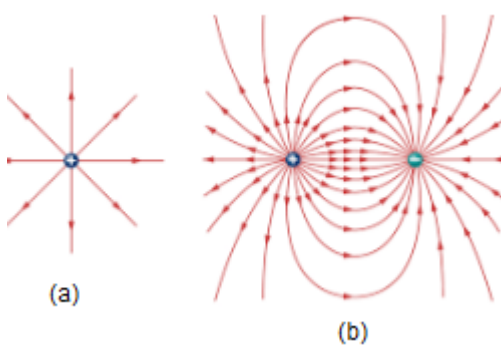
Explanation: Ozone layer lies in stratosphere.

(iv) (b) infrared

Explanation: The atmosphere of earth is richest in infrared radiation.

30. Read the text carefully and answer the questions:

Electric field lines as a path, straight or curved in an electric field such that tangent to it at any point gives the direction of electric field intensity at the point. Electric field lines are continuous curves they start from a positive charged body and end at the negatively charged body. (Refer image)



(i) (d) spherically symmetric

Explanation: spherically symmetric

(ii) (a) N/C

Explanation: N/C

(iii) (b) Electric field lines can intersect each other.

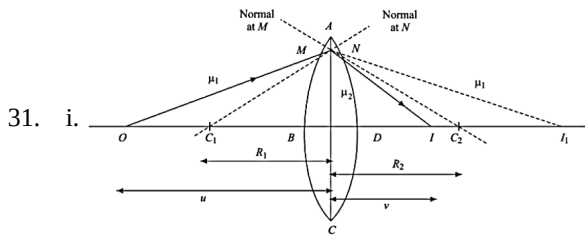
Explanation: Electric field lines can intersect each other.

- (iv) (a) path 'd'
Explanation: path 'd'

OR

- (c) All of these.
Explanation: All of these.

Section E



The complete derivation of the lens maker formula is described below. For refraction at surface ABC, we have

$$\frac{\mu_2}{v_1} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R_1} \dots(i) \quad (\text{Here } \mu_2, \mu_1 \text{ are the refractive index of the material})$$

For refraction at surface ADC, we have

$$\frac{\mu_1}{v} - \frac{\mu_2}{v_1} = \frac{\mu_1 - \mu_2}{R_2} \dots(ii)$$

Adding equation (i) and (ii), we get

$$\frac{\mu_1}{v} - \frac{\mu_1}{u} = (\mu_2 - \mu_1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\frac{1}{v} - \frac{1}{u} = \left[\frac{(\mu_2 - \mu_1)}{\mu_1} \right] \left[\frac{1}{R_1} - \frac{1}{R_2} \right] \dots(iii)$$

If the object is placed at infinity ($u = \infty$), the image will be formed at the focus, i.e. $v = f$

Therefore

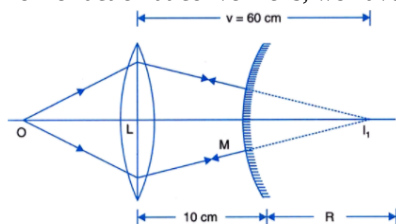
$$\frac{1}{f} - \frac{1}{\infty} = (\mu_{21} - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right] \dots(iv)$$

From eq. (iii) and (iv), we have

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

This is Lens maker formula.

- ii. For refraction at convex lens, we have



Object distance, $u = -12$ cm

Image distance, $v = ?$

Focal length, $f = +10$ cm

Using lens formula, we have

$$\frac{1}{v} - \frac{1}{(-12)} = \frac{1}{10}$$

i.e. $v = +60$ cm

Thus, in the absence of a convex mirror, the convex lens will form the image I_1 , at a distance of 60cm behind the lens. As the mirror is at a distance of 10cm from the lens, image I_1 will be at a distance of $(60 - 10) = 50$ cm from the mirror, i.e., $MI_1 = 50$ cm.

Now, as the final image I_2 is formed at the object itself, the rays after reflection from the mirror retrace its path, i.e., the rays on the mirror are incident normally, i.e., I_1 is the centre of the mirror so that

$$R = MI_1 = +50 \text{ cm}$$

$$\text{and } f = \frac{R}{2} = \frac{50}{2} = 25 \text{ cm}$$

Which is the focal length of the mirror.

OR

- i. There are two sets of apparatus of Young's double-slit experiment. In Set A: Stable interference pattern, the positions of maxima and minima do not change with time.

In Set B: Positions of maxima and minima will change rapidly with time and an average uniform intensity distribution will be observed on the screen.

ii. Expression for the intensity of stable interference pattern in set-A

If the displacement produced by slit S_1 is given by

$$y_1 = a \cos \omega t$$

then, the displacement produced by S_2 would be

$$y_2 = a \cos (\omega t + \phi)$$

and the resultant displacement will be given by

$$\begin{aligned} y &= y_1 + y_2 \\ &= a[\cos \omega t + \cos (\omega t + \phi)] \\ &= 2a \cos \left(\frac{\phi}{2}\right) \cos \left(\omega t + \frac{\phi}{2}\right) \end{aligned}$$

The amplitude of the resultant displacement is $2a \cos \left(\frac{\phi}{2}\right)$ and therefore the intensity at that point will be

$$I = 4I_0 \cos^2 \left(\frac{\phi}{2}\right)$$

$$\phi = 0$$

$$\therefore I = 4I_0$$

In set B, the intensity will be given by the average intensity is given by :-

$$I = 4I_0 \cos^2 \left(\frac{\phi}{2}\right)$$

$$I = 2I_0$$

32. $Q = Q_1 + Q_2$

$V_1 = V_2$ potential of both capacitors after they are connected with each other.

$$\therefore \frac{Q_1}{C_1} = \frac{Q_2}{C_2} \Rightarrow Q = \left(\frac{C_1}{C_2} + 1\right) Q_2$$

$$Q_2 = \frac{QC_2}{C_1 + C_2} \quad Q_1 = \frac{QC_1}{C_1 + C_2}$$

$$V_2 = V_1 = \frac{Q}{C_1 + C_2} = \frac{Q_2}{C_2} = \frac{Q_1}{C_1}$$

$$U_f = \frac{1}{2} C_1 V_1^2 + \frac{1}{2} C_2 V_2^2 = \frac{1}{2} (C_1 + C_2) \frac{Q^2}{(C_1 + C_2)^2} = \frac{Q^2}{2(C_1 + C_2)}$$

$$U_i = \frac{Q^2}{2C_1}$$

$$U_i - U_f = \frac{Q^2}{2C_1} - \frac{Q^2}{2(C_1 + C_2)} = \frac{Q^2(C_2)}{(C_1)(C_1 + C_2)}$$

The lost energy appears in the form of heat.

OR

Let $OA = OB = OC = OD = r$

Then the potential at the centre O is

$$V_O = \frac{1}{4\pi\epsilon_0} \left[\frac{q}{r} + \frac{q}{r} - \frac{q}{r} - \frac{q}{r} \right] = 0$$

Again, the potential at point E is

$$V_E = \frac{1}{4\pi\epsilon_0} \left[\frac{q}{AE} + \frac{q}{BE} - \frac{q}{CE} - \frac{q}{DE} \right] = 0 \quad [\because AE = DE, BE = CE]$$

$$\text{Now, } AF = BF = \sqrt{a^2 + \left(\frac{a}{2}\right)^2} = \frac{\sqrt{5}a}{2}$$

\therefore The potential at point F is

$$\begin{aligned} V_F &= \frac{1}{4\pi\epsilon_0} \left[\frac{q}{AF} + \frac{q}{BF} - \frac{q}{CF} - \frac{q}{DF} \right] \\ &= \frac{2q}{4\pi\epsilon_0} \left[\frac{1}{AF} - \frac{1}{CF} \right] \quad [\because AF = BF, CF = DF] \\ &= \frac{2q}{4\pi\epsilon_0} \left[\frac{2}{\sqrt{5}a} - \frac{2}{a} \right] = \frac{q}{\pi\epsilon_0 a} \left(\frac{1}{\sqrt{5}} - 1 \right) \end{aligned}$$

Work done in moving the charge V from O to E is $W = e[V_E - V_O] = e \times 0 = 0$

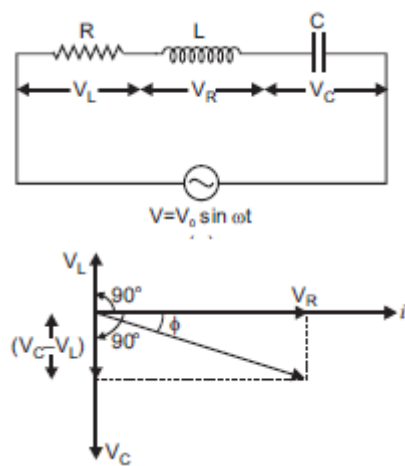
Work done in moving the charge 'e' from O to F is

$$\begin{aligned} W &= e[V_F - V_O] = e \left[\frac{q}{\pi\epsilon_0 a} \left(\frac{1}{\sqrt{5}} - 1 \right) - 0 \right] \\ &= \frac{qe}{\pi\epsilon_0 a} \left(\frac{1}{\sqrt{5}} - 1 \right) \end{aligned}$$

33. Suppose a resistance R , inductance L and capacitance C in series. An alternating source of voltage $V = V_0 \sin \omega t$ is applied across it. Since all the components are connected in series, the current flowing through all is same.

Voltage across resistance R is V_R , voltage across inductance L is V_L and voltage across capacitance C is V_C .

V_R and $(V_C - V_L)$ are mutually perpendicular and the phase difference between them is 90° .



From the figure above, we have

$$V^2 = V_R^2 + (V_C - V_L)^2 \Rightarrow V = \sqrt{V_R^2 + (V_C - V_L)^2} \dots (i)$$

and $V_R = Ri$, $V_C = X_C i$ and $V_L = X_L i \dots (ii)$

where $X_C = \frac{1}{\omega C}$ = capacitance reactance and $X_L = \omega L$ = inductive reactance

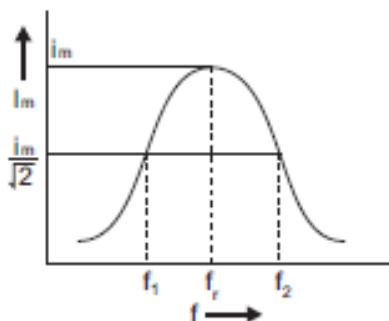
$$\therefore V = \sqrt{(Ri)^2 + (X_C i - X_L i)^2}$$

$$\therefore \text{Impedance of circuit, } Z = \frac{V}{i} = \sqrt{R^2 + (X_C - X_L)^2}$$

$$\text{i.e. } Z = \sqrt{R^2 + (X_C - X_L)^2} = \sqrt{R^2 + \left(\frac{1}{\omega C} - \omega L\right)^2}$$

The phase difference between current and voltage is given by,

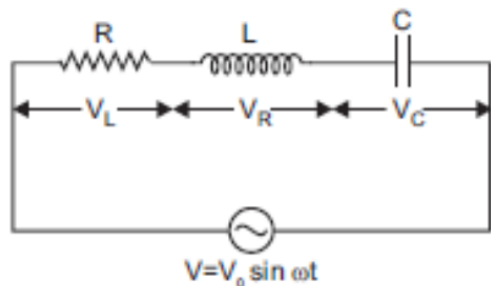
$$\tan \phi = \frac{X_C - X_L}{R}$$



From the graph, we can see that with increase in frequency, current first increases and then decreases. At resonant frequency, current amplitude is maximum.

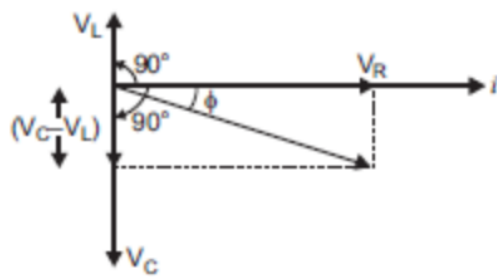
OR

- a. Suppose a resistance R, inductance L and capacitance C are connected to series and an alternating voltage $V = V_0 \sin \omega t$ is applied across it.



Since L, C and R are connected in series, current flowing through them is the same. The voltage across R is V_R , inductance across L is V_L and across capacitance is V_C .

The voltage V_R and current i are in the same phase, the voltage V_L will lead the current by angle 90° while the voltage V_C will lag behind the current by 90° .



Thus, V_R and $(V_C - V_L)$ are mutually perpendicular and the phase difference between them is 90° . As seen in the fig, we can say that, as the applied voltage across the circuit is V , the resultant of V_R and $V_C - V_L$ will also be V .

So,

$$V^2 = V_R^2 + (V_C - V_L)^2$$

$$\Rightarrow V = \sqrt{V_R^2 + (V_C - V_L)^2}$$

But, $V_R = Ri$, $V_C = X_C i$ and $V_L = X_L i$

where, $X_C = \frac{1}{\omega C}$ and $X_L = \omega L$

$$\text{So, } V = \sqrt{(Ri)^2 + (X_C i - X_L i)^2},$$

Therefore, impedance of the circuit is given by,

$$Z = \frac{V}{i} = \sqrt{(R)^2 + (X_C - X_L)^2}$$

$$Z = \sqrt{R^2 + \left(\frac{1}{\omega C} - \omega L\right)^2}$$

This is the impedance of the LCR series circuit.

- b. A radio or a TV set has an LC circuit capacitor of variable capacitance C . The circuit remains connected with an aerial coil through the phenomenon of mutual inductance. Suppose a radio or TV station has transmitted a program at frequency f , then waves produce an alternating voltage of frequency in area, due to which an emf of the same frequency is induced in LC circuit. When capacitor C in circuit is varied then for a particular value of capacitance, C , $f = \frac{1}{2\pi\sqrt{LC}}$, the resonance occurs and maximum current flows in the circuit; so the radio or TV gets tuned.